## CONGRUENCE THROUGH TRANSFORMATIONS

1. Triangle $A B C$ has vertices $A(-4,-2), B(-1,3)$, and $C(5,0)$.
a. Translate $\triangle \mathrm{ABC}$ down 3 units to form $\triangle A^{\prime} B^{\prime} C^{\prime}$. Graph $\triangle A^{\prime} B^{\prime} C^{\prime}$ on the same coordinate plane as $\triangle \mathrm{ABC}$.

b. What are the coordinates of the vertices of $\triangle A^{\prime} B^{\prime} C^{\prime}$ ?

The coordinates of $A^{\prime}$ are ( $\qquad$ ,__).

The coordinates of $B^{\prime}$ are ( __, ___ ).
The coordinates of $C^{\prime}$ are ( $\qquad$ , __ ).
c. How could you determine the coordinates of the vertices of the image without using a graph?
2. Consider the congruence statement $\triangle R U G \cong \triangle C A R$.
a. Identify the congruent sides.
b. Identify the congruent angles.
3. Triangle $D E F$ has vertices $D(-1,-3), E(3,2)$, and $F(6,0)$.
a. Translate $\triangle D E F 4$ units to the left to form $\triangle D^{\prime} E^{\prime} F^{\prime}$. Graph $\triangle D^{\prime} E^{\prime} F^{\prime}$ on the same coordinate plane as $\triangle D E F$.

b. What are the coordinates of the vertices of $\triangle D^{\prime} E^{\prime} F^{\prime}$ ?

The coordinates of $D^{\prime}$ are ( __, ___ ).
The coordinates of $E^{\prime}$ are (__, __ ).
The coordinates of $F^{\prime}$ are (__, __ ).
c. How could you determine the coordinates of the vertices of the image without using a graph?
4. Consider the congruence statement $\triangle S U N \cong \triangle F O G$.
a. Identify the congruent sides.
b. Identify the congruent angles.
5. Triangle $D E F$ has vertices $D(-3,5), E(1,-3)$, and $F(-6,-4)$.
a. Translate $\triangle D E F 2$ units to the right and 3 units up to form $\triangle D^{\prime} E^{\prime} F^{\prime}$. Graph
$\triangle D^{\prime} E^{\prime} F^{\prime}$ on the same coordinate plane as $\triangle D E F$.

b. What are the coordinates of the vertices of $\triangle D^{\prime} E^{\prime} F^{\prime}$ ?

The coordinates of $D^{\prime}$ are ( __ , __ ).
The coordinates of $E^{\prime}$ are ( $\qquad$ , __ ) ).

The coordinates of $F^{\prime}$ are ( $\qquad$
c. How could you determine the coordinates of the vertices of the image without using a graph?
6. Consider the congruence statement $\triangle R A T \cong \triangle H O G$.
a. Identify the congruent sides.
7. Triangle $A B C$ has vertices $A(-4,-2), B(-1,3)$, and $C(5,0)$.
a. Rotate $\triangle A B C 180^{\circ}$ counterclockwise about the origin to form $\triangle A^{\prime} B^{\prime} C^{\prime}$. Graph $\triangle A^{\prime} B^{\prime} C^{\prime}$ on the same coordinate plane as $\triangle A B C$.

b. What are the coordinates of the vertices of $\triangle A^{\prime} B^{\prime} C^{\prime}$ ?

The coordinates of $A^{\prime}$ are ( $\qquad$ , $\qquad$ ).

The coordinates of $B^{\prime}$ are ( $\qquad$ , $\qquad$ ).

The coordinates of $C^{\prime}$ are ( $\qquad$ , $\qquad$ ).
c. How could you determine the coordinates of the vertices of the image without using a graph?
b. Identify the congruent angles.

Write the congruence statements represented by the markers in each diagram.
8.


Congruence Statement: $\qquad$
9.


Congruence Statement: $\qquad$
10. For the figure shown, which is a correct congruence statement?

a. $\triangle M N O \cong \triangle P Q O$
b. $\triangle N O M \cong \triangle P Q O$
c. $\triangle M N O \cong \triangle Q P O$
d. $\triangle M O N \cong \triangle P O Q$
11. If $\triangle D E F \cong \triangle L K J$, which congruence statement is not necessarily correct?
a. $\angle E \cong \angle K$
b. $\overline{D E} \cong \overline{J K}$
c. $\angle F \cong \angle J$
d. $\overline{D F} \cong \overline{L J}$
12. Dianne drew a triangle with vertices (1, 3), (3, 2), and $(4,2)$. She also drew an image of this triangle whose vertices had coordinates $(-1,3),(-3,2)$ and $(-4,2)$. How did she make the image?
a. She translated the original triangle 2 units down.
b. She translated the original triangle 6 units down.
c. She reflected the original triangle over the $x$-axis.
d. She reflected the original triangle over the $y$-axis.
13. If $\triangle C A T \cong \triangle D O G$, which statement must be true?
a. $m \angle A=m \angle O$
b. $\angle C \cong \angle G$
c. $\quad C A=O G$
d. $\overline{C T} \cong \overline{D O}$
14. Which transformation was used to create $\triangle D E F$ from $\triangle A B C$ ?

a. $\triangle A B C$ was reflected over the $y$-axis.
b. $\triangle A B C$ was translated to the right 3 units and down 1 unit.
c. $\triangle A B C$ was rotated 90 clockwise about the origin.
d. $\triangle A B C$ was translated to the right 1 unit and down 3 units.
15. Regina drew a triangle with vertices $(1,2),(3,3)$, and $(4,1)$. She translated the triangle 2 units down to create an image. What are the vertices of the image?
a. $(1,0),(3,1)$, and $(4,-1)$
b. $(1,4),(3,5)$, and $(4,3)$
c. $(-1,2),(1,3)$, and $(2,1)$
d. $(3,2),(5,3)$, and $(6,1)$
16. Logan drew $\triangle A B C$ on the coordinate plane, and then reflected the triangle over the y -axis to form $\Delta A^{\prime} B^{\prime} C^{\prime}$. Which statement is not true about these two triangles?
a. $\triangle A B C \cong \triangle A^{\prime} B^{\prime} C^{\prime}$
b. The two triangles have the same angle measures.
c. The vertices of $\triangle A B C$ and $\triangle A^{\prime} B^{\prime} C^{\prime}$ have the same coordinates.
d. The triangles have the same side lengths.
17. Samantha drew $\triangle J K L$ with vertices $(2,3),(4,3)$, and $(5,2)$. She reflected this triangle over the $x$-axis to create an image. What are the coordinates of the vertices of the image?
a. $(0,3),(2,3)$, and $(3,2)$
b. $(2,0),(4,0)$, and $(5,-1)$
c. $(-2,3),(-4,3)$, and $(-5,2)$
d. $(2,-3),(4,-3)$, and $(5,-2)$
18. Henry draws $\triangle F G H$. Then, he translates that triangle to create $\Delta F^{\prime} G^{\prime} H^{\prime}$. The distance from $F$ to $F^{\prime}$ is 4 centimeters. What is the length of $\overline{G G^{\prime}}$ ?
a. 2 centimeters
b. 3 centimeters
c. 4 centimeters
d. 6 centimeters
19. Which transformation was used to create $\triangle G H I$ from $\triangle D E F$ ?

a. $\triangle D E F$ was rotated $90^{\circ}$ counterclockwise about the origin.
b. $\triangle D E F$ was rotated $180^{\circ}$ counterclockwise about the origin.
c. $\triangle D E F$ was translated over the $x$-axis.
d. $\triangle D E F$ was translated over the $y$-axis.
20. If the point $(-5,8)$ is rotated $90^{\circ}$ counterclockwise about the origin, what will be the coordinates of the rotated point?
a. $(5,-8)$
b. $(-8,5)$
c. $(5,8)$
d. $(-8,-5)$

# Congruence Through Transformations ANSWER KEY 

## Answer Section

1. ANS:
a.

b. The coordinates of $A^{\prime}$ are $(-4,-5)$.

The coordinates of $B^{\prime}$ are $(-1,0)$.
The coordinates of $C^{\prime}$ are $(5,-3)$.
c. The coordinates of the vertices of the image could be determined by subtracting 3 from each of the $y$-coordinates of the vertices of the original triangle. The $x$-coordinates stay the same.

REF: 8.1
2. ANS:
a. $\overline{R U} \cong \overline{C A}$
$\overline{U G} \cong \overline{A R}$
$\overline{R G} \cong \overline{C R}$
b. $\angle R \cong \angle C$
$\angle U \cong \angle A$
$\angle G \cong \angle R$
REF: 8.2
3. ANS:
a.

b. The coordinates of $D^{\prime}$ are $(-5,-3)$.

The coordinates of $E^{\prime}$ are $(-1,2)$.
The coordinates of $F^{\prime}$ are (2,0).
c. The coordinates of the vertices of the image could be determined by subtracting 4 from each of the $x$-coordinates of the vertices of the original triangle. The $y$-coordinates stay the same.

REF: 8.1
4. ANS:
a. $\overline{S U} \cong \overline{F O}$

$$
\overline{U N} \cong \overline{O G}
$$

$$
\overline{S N} \cong \overline{F G}
$$

b. $\angle S \cong \angle F$
$\angle U \cong \angle O$
$\angle N \cong \angle G$
REF: 8.2
5. ANS:
a.

b. The coordinates of $D^{\prime}$ are $(-1,8)$.

The coordinates of $E^{\prime}$ are $(3,0)$.
The coordinates of $F^{\prime}$ are $(-4,-1)$.
c. The coordinates of the vertices of the image could be determined by adding 2 to each of the $x$-coordinates and adding 3 to each of the $y$-coordinates of the original triangle.

REF: 8.1
6. ANS:
a. $\overline{R A} \cong \overline{H O}$
$\overline{A T} \cong \overline{O G}$
$\overline{R T} \cong \overline{H G}$
b. $\angle R \cong \angle H$
$\angle A \cong \angle O$
$\angle T \cong \angle G$

REF: 8.2
7. ANS:
a.

b. The coordinates of $A^{\prime}$ are $(4,2)$.

The coordinates of $B^{\prime}$ are $(1,-3)$.
The coordinates of $C^{\prime}$ are $(-5,0)$.
c. The coordinates of the vertices of the image could be determined by writing the opposite of each of the $x$-coordinates and writing the opposite of each of the $y$-coordinates of the vertices of the original triangle.

REF: 8.1
8. ANS:
$\angle H G I \cong \angle H F J$ and $\overline{H I} \cong \overline{I J}$
REF: 8.2
9. ANS:
$\overline{R S} \cong \overline{V U}, \overline{S T} \cong \overline{U T}$, and $\angle S \cong \angle U$
REF: 8.2
10. ANS: C

REF: 8.2
11. ANS: B

REF: 8.2
12. ANS: D

REF: 8.1
13. ANS: A

REF: 8.2
14. ANS: B

REF: 8.1
15. ANS: A

REF: 8.1
16. ANS: C

REF: 8.1
17. ANS: D

REF: 8.1
18. ANS: C

REF: 8.1
19. ANS: B

REF: 8.1
20. ANS: D

REF: 8.1

